

May 19, 2018 at 02:30

1. Intro. This little program outputs clauses that are satisfiable if and only if the graph g can be c -colored, given g and c . It differs from SAT-COLOR-LOG because it uses a different way to compare binary labels.

Suppose the graph has m edges and n vertices, and let $t = \lceil \lg c \rceil$. Then there are nt variables $v.k$, meaning that vertex v gets color $(v.1 v.2 \dots v.t)_2$.

There are cm clauses of size $2t$ to ensure that adjacent vertices don't share a color. And there are $O(nt)$ additional clauses of size $\leq t$, to rule out cases where a vertex is assigned to colors s in the range $n \leq s < 2^t$.

```
#include <stdio.h>
#include <stdlib.h>
#include "gb_graph.h"
#include "gb_save.h"
int c;
main(int argc, char *argv[])
{
    register int i, k, t;
    register Arc *a;
    register Graph *g;
    register Vertex *u, *v;
    <Process the command line 2>;
    for (t = 0; c > (1 << t); t++) ;
    <Generate negative clauses to rule out bad colors 3>;
    for (v = g->vertices; v < g->vertices + g->n; v++)
        for (a = v->arcs; a; a = a->next) {
            u = a->tip;
            if (u < v) <Generate clauses to keep u and v from having the same color 4>;
        }
}
```

```
2. <Process the command line 2> ≡
if (argc ≠ 3 ∨ sscanf(argv[2], "%d", &c) ≠ 1) {
    fprintf(stderr, "Usage: %s s foo.gb c\n", argv[0]);
    exit(-1);
}
g = restore_graph(argv[1]);
if (¬g) {
    fprintf(stderr, "I couldn't reconstruct graph %s!\n", argv[1]);
    exit(-2);
}
if (c ≤ 0) {
    fprintf(stderr, "c must be positive!\n");
    exit(-3);
}
printf("~ sat-color-log2 %s %d\n", argv[1], c);
```

This code is used in section 1.

3. \langle Generate negative clauses to rule out bad colors 3 $\rangle \equiv$

```

for ( $i = 0$ ;  $i < t$ ;  $i++$ )
  if ( $((c - 1) \& (1 \ll i)) \equiv 0$ ) {
    for ( $v = g\text{-vertices}$ ;  $v < g\text{-vertices} + g\text{-n}$ ;  $v++$ ) {
       $\text{printf}(\text{"\%s.\%d"}, v\text{-name}, t - i)$ ;
      for ( $k = i + 1$ ;  $k < t$ ;  $k++$ )
        if ( $(c - 1) \& (1 \ll k)$ )  $\text{printf}(\text{"\_%s.\%d"}, v\text{-name}, t - k)$ ;
       $\text{printf}(\text{"\n"})$ ;
    }
  }

```

This code is used in section 1.

4. \langle Generate clauses to keep u and v from having the same color 4 $\rangle \equiv$

```

{
  for ( $k = 0$ ;  $k < c$ ;  $k++$ ) {
    for ( $i = 0$ ;  $i < t$ ;  $i++$ )
      if ( $k \& (1 \ll i)$ )  $\text{printf}(\text{"\_%s.\%d\_%s.\%d"}, u\text{-name}, t - i, v\text{-name}, t - i)$ ;
      else  $\text{printf}(\text{"\_%s.\%d\_%s.\%d"}, u\text{-name}, t - i, v\text{-name}, t - i)$ ;
       $\text{printf}(\text{"\n"})$ ;
    }
  }
}

```

This code is used in section 1.

5. Index.*a*: 1.**Arc**: 1.*ares*: 1.*argc*: 1, 2.*argv*: 1, 2.*c*: 1.*exit*: 2.*fprintf*: 2.*g*: 1.**Graph**: 1.*i*: 1.*k*: 1.*main*: 1.*name*: 3, 4.*next*: 1.*printf*: 2, 3, 4.*restore_graph*: 2.*sscanf*: 2.*stderr*: 2.*t*: 1.*tip*: 1.*u*: 1.*v*: 1.**Vertex**: 1.*vertices*: 1, 3.

- ⟨Generate clauses to keep u and v from having the same color 4⟩ Used in section 1.
- ⟨Generate negative clauses to rule out bad colors 3⟩ Used in section 1.
- ⟨Process the command line 2⟩ Used in section 1.

SAT-COLOR-LOG2

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