

1. **Intro.** Supplementary clauses to speed up `sat-color-order queen $n \times n$.gb` d : These clauses say that every k -clique must contain at least one relatively high color and at least one relative low color.

```
#include <stdio.h>
#include <stdlib.h>
int n; /* this many queens */
int d; /* this many colors */
main(int argc, char *argv[])
{
    register int i, j, k, l;
    <Process the command line 2>;
    <Generate the clauses 3>;
}

2. <Process the command line 2> ≡
if (argc ≠ 3 ∨ sscanf(argv[1], "%d", &n) ≠ 1 ∨ sscanf(argv[2], "%d", &d) ≠ 1) {
    fprintf(stderr, "Usage: %s %d\n", argv[0]);
    exit(-1);
}
if (d < n) {
    fprintf(stderr, "The number of colors (%d) must be at least %d!\n", d, n);
    exit(-2);
}
printf("~ %s %d %d\n", n, d);
```

This code is used in section 1.

```
3. <Generate the clauses 3> ≡
for (k = 0; k < n; k++) {
    <Generate cliques for row k 4>;
    <Generate cliques for column k 5>;
}
for (k = 1; k ≤ n + n - 3; k++) <Generate cliques for i + j = k 6>;
for (k = 2 - n; k ≤ n - 2; k++) <Generate cliques for i - j = k 7>;
```

This code is used in section 1.

```
4. <Generate cliques for row k 4> ≡
{
    for (j = 0; j < n; j++) printf("%d.%d<%d", k, j, d - n + 1);
    printf("\n");
    for (j = 0; j < n; j++) printf("~%d.%d<%d", k, j, n - 1);
    printf("\n");
}
```

This code is used in section 3.

```
5. <Generate cliques for column k 5> ≡
{
    for (j = 0; j < n; j++) printf("%d.%d<%d", j, k, d - n + 1);
    printf("\n");
    for (j = 0; j < n; j++) printf("~%d.%d<%d", j, k, n - 1);
    printf("\n");
}
```

This code is used in section 3.

```

6. ⟨Generate cliques for  $i + j = k - 6$ ⟩ ≡
{
  if ( $k < n$ ) {
     $l = k + 1$ ;
    for ( $i = 0; i \leq k; i++$ ) printf("%d.%d<%d",  $i, k - i, d - l + 1$ );
    printf("\n");
    for ( $i = 0; i \leq k; i++$ ) printf("%d.%d<%d",  $i, k - i, l - 1$ );
    printf("\n");
  } else {
     $l = n + n - 1 - k$ ;
    for ( $i = n - l; i < n; i++$ ) printf("%d.%d<%d",  $i, k - i, d - l + 1$ );
    printf("\n");
    for ( $i = n - l; i < n; i++$ ) printf("%d.%d<%d",  $i, k - i, l - 1$ );
    printf("\n");
  }
}

```

This code is used in section 3.

```

7. ⟨Generate cliques for  $i - j = k - 7$ ⟩ ≡
{
  if ( $k > 0$ ) {
     $l = n - k$ ;
    for ( $i = k; i < n; i++$ ) printf("%d.%d<%d",  $i, i - k, d - l + 1$ );
    printf("\n");
    for ( $i = k; i < n; i++$ ) printf("%d.%d<%d",  $i, i - k, l - 1$ );
    printf("\n");
  } else {
     $l = n + k$ ;
    for ( $i = 0; i < n + k; i++$ ) printf("%d.%d<%d",  $i, i - k, d - l + 1$ );
    printf("\n");
    for ( $i = 0; i < n + k; i++$ ) printf("%d.%d<%d",  $i, i - k, l - 1$ );
    printf("\n");
  }
}

```

This code is used in section 3.

8. Index.*argc*: 1, 2.*argv*: 1, 2.*d*: 1.*exit*: 2.*fprintf*: 2.*i*: 1.*j*: 1.*k*: 1.*l*: 1.*main*: 1.*n*: 1.*printf*: 2, 4, 5, 6, 7.*scanf*: 2.*stderr*: 2.

- ⟨ Generate cliques for column k 5 ⟩ Used in section 3.
- ⟨ Generate cliques for row k 4 ⟩ Used in section 3.
- ⟨ Generate cliques for $i + j = k$ 6 ⟩ Used in section 3.
- ⟨ Generate cliques for $i - j = k$ 7 ⟩ Used in section 3.
- ⟨ Generate the clauses 3 ⟩ Used in section 1.
- ⟨ Process the command line 2 ⟩ Used in section 1.

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