

1. Intro. Generate SAT instances for van der Waerden configurations: There are to be no k equally spaced zeroes and no l equally spaced ones, in a binary string of length n . (If unsatisfiable, every red-green coloring of $\{1, 2, \dots, n\}$ contains a red arithmetic progression of length k or a green arithmetic progression of length l .)

The numbers k, l, n are given on the command line.

```
#include <stdio.h>
#include <stdlib.h>
int k, l, n;
main(int argc, char *argv[])
{
    register int i, j, d;
    <Process the command line 2>;
    <Output the positive clauses 3>;
    <Output the negative clauses 4>;
}
```

2. <Process the command line 2> \equiv

```
if (argc  $\neq$  4  $\vee$  sscanf(argv[1], "%d", &k)  $\neq$  1  $\vee$  sscanf(argv[2], "%d", &l)  $\neq$  1  $\vee$  sscanf(argv[3], "%d", &n)  $\neq$  1)
{
    fprintf(stderr, "Usage: %s k l n\n", argv[0]);
    exit(-1);
}
printf("~ sat-waerden %d %d %d\n", k, l, n);
```

This code is used in section 1.

3. <Output the positive clauses 3> \equiv

```
for (d = 1; 1 + (k - 1) * d  $\leq$  n; d++) {
    for (i = 1; i + (k - 1) * d  $\leq$  n; i++) {
        for (j = 0; j < k; j++) printf("%d", i + j * d);
        printf("\n");
    }
}
```

This code is used in section 1.

4. <Output the negative clauses 4> \equiv

```
for (d = 1; 1 + (l - 1) * d  $\leq$  n; d++) {
    for (i = 1; i + (l - 1) * d  $\leq$  n; i++) {
        for (j = 0; j < l; j++) printf("%d", i + j * d);
        printf("\n");
    }
}
```

This code is used in section 1.

5. Index.*argc*: 1, 2.*argv*: 1, 2.*d*: 1.*exit*: 2.*fprintf*: 2.*i*: 1.*j*: 1.*k*: 1.*l*: 1.*main*: 1.*n*: 1.*printf*: 2, 3, 4.*scanf*: 2.*stderr*: 2.

- ⟨Output the negative clauses 4⟩ Used in section 1.
- ⟨Output the positive clauses 3⟩ Used in section 1.
- ⟨Process the command line 2⟩ Used in section 1.

SAT-WAERDEN

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