

1* Intro. This quickie outputs clauses that are unsatisfiable because they state that there exists a partial ordering on m elements in which no element is maximal. (All backtrack proofs of this fact are known to require $\Omega(2^m)$ steps.)

Variable $j.k$ means that $j \prec k$ in the partial ordering.

This variant uses only the special cases of transitivity where $i < j$ and $k < j$.

```
#include <stdio.h>
#include <stdlib.h>
int m;
main(int argc, char *argv[])
{
    register i, j, k;
    <Process the command line 2*>;
    <Generate the clauses for irreflexivity 3>;
    <Generate the clauses for transitivity 4*>;
    <Generate the clauses for nonmaximality 5>;
}

2* <Process the command line 2*> ≡
if (argc ≠ 2 ∨ sscanf(argv[1], "%d", &m) ≠ 1) {
    fprintf(stderr, "Usage: %s %d\n", argv[0]);
    exit(-1);
}
printf("~ %sat-poset-nomax-a %d\n", m);
```

This code is used in section 1*.

```
3. <Generate the clauses for irreflexivity 3> ≡
for (j = 1; j ≤ m; j++) printf("~%d.%d\n", j, j);
```

This code is used in section 1*.

```
4* <Generate the clauses for transitivity 4*> ≡
for (i = 1; i ≤ m; i++)
    for (j = 1; j ≤ m; j++)
        if (i < j) {
            for (k = 1; k ≤ m; k++)
                if (k < j) {
                    printf("~%d.%d~%d.%d\n", i, j, j, k, i, k);
                }
        }
}
```

This code is used in section 1*.

```
5. <Generate the clauses for nonmaximality 5> ≡
for (j = 1; j ≤ m; j++) {
    for (k = 1; k ≤ m; k++) printf("%d.%d", j, k);
    printf("\n");
}
```

This code is used in section 1*.

6* Index.

The following sections were changed by the change file: 1, 2, 4, 6.

argc: 1*, 2*

argv: 1*, 2*

exit: 2*

fprintf: 2*

i: 1*

j: 1*

k: 1*

m: 1*

main: 1*

printf: 2*, 3, 4*, 5.

scanf: 2*

stderr: 2*

- ⟨Generate the clauses for irreflexivity 3⟩ Used in section 1*.
- ⟨Generate the clauses for nonmaximality 5⟩ Used in section 1*.
- ⟨Generate the clauses for transitivity 4*⟩ Used in section 1*.
- ⟨Process the command line 2*⟩ Used in section 1*.

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