1* Intro. This program reads in a `.dots` file (see SAT-LIFE) and outputs clauses that will be satisfiable if and only if the 1s can be covered with dominoes having no three sharing a vertex. (Notice that I said 'no three', not 'no four'. This condition affects patterns with internal holes.)

Well, no: This variant simply asks for an exact covering by dominoes. And instead of reading a `dots` file, it works with an $m \times n$ chessboard, minus two cells on opposite corners.

The variables are i`H`j and i`V`j, meaning that pixel (i, j) is occupied by the left half of a horizontal domino or the top half of a vertical domino, respectively.

```
#define maxx 50 /* maximum number of lines in the pattern supplied by stdin */
#define maxy 200 /* maximum number of columns per line in stdin */
#include <stdio.h>
#include <stdlib.h>
  char p[maxx + 2][maxy + 2]; /* is cell (x, y) potentially alive? */
  int xmax, ymax; /* the number of rows and columns in the input pattern */
  int xmin = maxx, ymin = maxy; /* limits in the other direction */
  char buf[maxy + 2]; /* input buffer */
  char a[4][8]; /* place to assemble clauses */
  main(int argc, char *argv[])
  {
    register int i, j, k, x, y;
    ⟨ Process the command line 5* ⟩;
    printf("~ sat-tatami-mutilated %d %d\n", xmax, ymax);
    ⟨ Generate the clauses for domino covering 3 ⟩;
  }
```

2. ⟨ Input the pattern 2 ⟩ ≡

```
  for (x = 1; ; x++) {
    if (¬fgets(buf, maxy + 2, stdin)) break;
    if (x > maxx) {
      fprintf(stderr, "Sorry, the pattern should have at most %d rows!\n", maxx);
      exit(−3);
    }
    for (y = 1; buf[y − 1] ≠ '\n'; y++) {
      if (y > maxy) {
        fprintf(stderr, "Sorry, the pattern should have at most %d columns!\n", maxy);
        exit(−4);
      }
      if (buf[y − 1] ≡ '*') {
        p[x][y] = 1;
        if (y > ymax) ymax = y;
        if (y < ymin) ymin = y;
        if (x > xmax) xmax = x;
        if (x < xmin) xmin = x;
      } else if (buf[y − 1] ≠ '.') {
        fprintf(stderr, "Unexpected character '%c' found in the pattern!\n", buf[y − 1]);
        exit(−5);
      }
    }
  }
```

3. Here I treat x as a row number and y as a column number. (Thus it's matrix notation, not Cartesian coordinates.)

```
⟨ Generate the clauses for domino covering 3 ⟩ ≡
  for (x = xmin; x ≤ xmax; x++)
    for (y = ymin; y ≤ ymax; y++)
      if (p[x][y]) {
        k = 0;
        if (p[x][y+1]) sprintf(a[k], "%dH%d", x, y), k++;
        if (p[x][y-1]) sprintf(a[k], "%dH%d", x, y-1), k++;
        if (p[x+1][y]) sprintf(a[k], "%dV%d", x, y), k++;
        if (p[x-1][y]) sprintf(a[k], "%dV%d", x-1, y), k++;
        if (k ≡ 0) {
          fprintf(stderr, "Cell␣(%d,", x);
          fprintf(stderr, "%d)␣cannot␣be␣covered␣with␣a␣domino!\n", y);
          exit(-1);
        }
        for (i = 0; i < k; i++)
          for (j = i+1; j < k; j++) printf("~%s␣~%s\n", a[i], a[j]);      /* prevent overlap */
        for (i = 0; i < k; i++) printf("␣%s", a[i]);
        printf("\n");      /* force covering */
      }
```

This code is used in section 1*.

4. ⟨ Generate the clauses to assert the tatami condition 4 ⟩ ≡

```
  for (x = xmin; x < xmax; x++)
    for (y = ymin; y < ymax; y++) {
      k = p[x][y] + p[x][y+1] + p[x+1][y] + p[x+1][y+1];
      if (k ≥ 3) {
        if (p[x][y] ∧ p[x][y+1]) printf("␣%dH%d", x, y);
        if (p[x][y] ∧ p[x+1][y]) printf("␣%dV%d", x, y);
        if (p[x+1][y] ∧ p[x+1][y+1]) printf("␣%dH%d", x+1, y);
        if (p[x][y+1] ∧ p[x+1][y+1]) printf("␣%dV%d", x, y+1);
        printf("\n");
      }
    }
```

5* ⟨ Process the command line 5* ⟩ ≡

```
if (argc ≠ 3 ∨ sscanf(argv[1], "%d", &xmax) ≠ 1 ∨ sscanf(argv[2], "%d", &ymax) ≠ 1) {
  fprintf(stderr, "Usage: %s m n\n", argv[0]);
  exit(−1);
}
if (xmax > maxx) {
  fprintf(stderr, "Sorry, the pattern should have at most %d rows!\n", maxx);
  exit(−3);
}
if (ymax > maxy) {
  fprintf(stderr, "Sorry, the pattern should have at most %d columns!\n", maxy);
  exit(−4);
}
xmin = ymin = 1;
for (x = 1; x ≤ xmax; x++)
  for (y = 1; y ≤ ymax; y++)
    if ((x ≠ 1 ∨ y ≠ ymax) ∧ (x ≠ xmax ∨ y ≠ 1)) p[x][y] = 1;
```

This code is used in section 1*.

6* Index.

The following sections were changed by the change file: 1, 5, 6.

⟨ Generate the clauses for domino covering 3 ⟩ Used in section 1*.
⟨ Generate the clauses to assert the tatami condition 4 ⟩
⟨ Input the pattern 2 ⟩
⟨ Process the command line 5* ⟩ Used in section 1*.

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